



# MANICALAND STATE UNIVERSITY OF APPLIED SCIENCES

FACULTY OF ENGINEERING, APPLIED SCIENCES &  
TECHNOLOGY

DEPARTMENT OF APPLIED STATISTICS

MODULE: REGRESSION AND ANOVA II

CODE: HAST 423

SESSIONAL EXAMINATIONS

APRIL 2023

DURATION: 3 HOURS

EXAMINER: NYAKUAMBA T

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## *INSTRUCTIONS*

1. Answer **All** in Section A
2. Answer **three** questions in Section B.
3. Start a new question on a fresh page
4. Total marks 100

**Additional material(s):** Non-programmable electronic scientific calculator,  
Statistical Tables

**SECTION A (40 MARKS)**

**ANSWER ALL QUESTIONS**

A1 (a) What is meant by regression analysis? [3]

(b) What justifies the inclusion of a disturbance or error term in regression analysis? [3]

A2. What do you understand by the following terms as used in regression analysis?

(a) autocorrelation [3]

(b) responds variable [3]

(c) leverage point [3]

(d) predictor [3]

(e) coefficient of determination [3]

A3 Suppose you have a regression model of the form

$$Y = a + bXi + ei \quad \{ i = 1,2, \dots n \}$$

(a) state the assumption underlying this model [5]

(b) derive the least square estimates of the two parameters and show that both are unbiased. [6, 8]

**SECTION B (60 marks)**

**Attempt any 3 Questions being careful to number them from B4 to B7**

B4. Draw a scatter plot diagram of two variables that

(a). are typically almost uncorelated [2]

(b). have a correlation coefficient close to 1

[2]

(c). have a correlation coefficient close to -1

[2]

(d). Prove that, if two random variables  $X$  and  $Y$  are such that  $y = a + bX$

(Where  $a$  and  $b$  are constants), then  $\rho_{xy} = +1$  or  $-1$

[4]

(e). Let two random variables  $X$  and  $Y$  have correlation coefficient  $\rho_{xy}$ ,

Prove that  $-1 \leq \rho_{xy} \leq 1$

[10]

B5.

A scientist collects experimental data on the radius of a propellant grain  $Y$ , as a function of powder temperature  $X_1$  and extension rate  $X_2$ .

He took 5 observations of each variable and the data is as follows

Y	25	30	28	32	40
X1	40	20	15	32	28
X2	20	15	15	24	20

Suppose the data can be described by the model

$$Y_i = b_0 + b_1X_i + b_2X_2 + e_i$$

Where  $e_i$  follows  $N(0, \sigma^2)$  and  $cov(e_i, e_j) = 0$  if  $i \neq j$

(a). express the model in matrix form

[2]

(b). obtain the decision matrix and calculate

$$X'Y \text{ and } X'X$$

[1, 3, 3]

(c). calculate the least squares estimate of  $b$  given that

$$(X'X)^{-1} = \begin{bmatrix} 1.165 & -0.134 & -0.180 \\ -0.134 & 0.0041 & 0.0049 \\ -0.180 & 0.0049 & 0.0156 \end{bmatrix}$$

(i). calculate the hat matrix H and explain its importance in regression

[3, 4]

(ii).test the hypothesis that  $H_0: \beta_1 = 0$  versus  $H_1: \beta_1 \neq 0$

use  $\alpha = 0.10$  and  $MSE = 7.815$

[4]

B6. Use the following data to answer the following questions:

X	22	68	108	137	255	315	390	405	685	700	1100
y	0.756	2.4	3.2	4.7	9.3	12.0	13.4	14.4	24.5	26.00	38.0

I. Plot the data above and comment.

[5]

II. Fit the model above

[4]

III. Do you think the above model is the best?

Support your answer

[4]

IV. State the assumptions satisfied by this model

[3]

V. Estimate the error variance

[4]

B7. Discuss the problems of

I. Multicollinearity in multiple regression.

(a) What it is

[2]

(b) How it affects regression analysis

[5]

(c) What could be done about it

[3]

ii. (a) Distinguish between step-wise regression and forward selection

approach to regression

[3]

(b) Explain the use of step wise regression

[3]

(c) Outline what is involved in the analysis of residuals.

[4]

**END OF EXAMINATION PAPER**