



**MANICALAND STATE UNIVERSITY  
OF  
APPLIED SCIENCES**

**FACULTY OF ENGINEERING**

**DEPARTMENT OF MINING AND MINERAL PROCESSING  
ENGINEERING  
DEPARTMENT OF CHEMICAL AND PROCESSING  
ENGINEERING**

**MODULE: ENGINEERING MATHEMATICS I**

**CODE: ENGT 102**

**SESSIONAL EXAMINATIONS**

**JUNE 2023**

**DURATION: 3 HOURS**

**EXAMINER: NYAKUAMBA T**

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***INSTRUCTIONS***

1. Answer **All** in Section A
2. Answer **three** questions in Section B.
3. Start a new question on a fresh page
4. Total marks 100

***Additional material(s): Non-programmable electronic scientific calculator.***

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**SECTION A (40 marks)**

**Answer ALL Questions**

A1. a) Does the decimal number 0.12345678910111213141516171819... represents a rational or an irrational number? Give a reason for your answer [3]

b) For what values of x is each of the following functions continuous

(i)  $f(x) = \frac{x^2}{x^2-1}$  [2]

(ii)  $f(x) = \frac{1+\cos x}{3+\sin x}$  [1]

(iii)  $f(x) = \frac{x-|x|}{x}$  [2]

A2 Let  $f(x) = \begin{cases} \frac{|x-3|}{x-3} & ; x \neq 3 \\ 0 & ; x = 3 \end{cases}$

(a) Graph the function  $f(x)$  [3]

(b) Find the  $\lim_{x \rightarrow 3^+} f(x)$  [2]

(c) Find the  $\lim_{x \rightarrow 3^-} f(x)$  [2]

(d) Find the  $\lim_{x \rightarrow 3} f(x)$  [1]

A3. IF  $X = -4, y = 10, z = 3$

$P = 2/3, q = 5/4$  and  $r = -4/5$

(a) Evaluate: (i)  $(x+y)+z$

(ii)  $x+(y+z)$  [2]

(b) .Evaluate (i)  $(pq)r$

(ii)  $p(qr)$  [2]

(c). which law is illustrated by the two questions a and b above [2]

(d).You are told that  $\pi = 22/7$  is this true or false. Give reason for your answer

[2]

A4. Differentiate the following functions with respect to x

(i)  $f(x) = x^2 - \frac{1}{\sqrt{x}} + \ln x$  [2]

(ii)  $x^2 - xy + y^2 = 0$  [3]

(iii)  $x = \cos 2t; y = \sin 2t$  [3]

A5). Find the set of values of  $x$  for which the following set of inequalities hold

(a)  $|x + 2| \geq |x - 3|$  [4]

(b)  $\frac{2}{7x} - 1 > \frac{4}{3x}$  [4]

**SECTION B. (60 Marks)**

**Candidate may attempt three questions being careful to number them B6 to B9**

B6. (i) Evaluate the following limits

a)  $\lim_{n \rightarrow \infty} \frac{n^2 + n}{n^3 - n^2}$

b)  $\lim_{n \rightarrow \infty} \frac{2n + 2}{3n - 5}$

c)  $\lim_{n \rightarrow 0} \frac{\sin x}{x}$

d)  $\lim_{x \rightarrow 5} 3$

e)  $\lim_{n \rightarrow \infty} (\sqrt{n + 10} - \sqrt{n})$

[2,2,2,2,4]

(ii) Solve the following equations

(a)  $|3 + 2x| = 2|x + 1|$  [4]

(b)  $\frac{2}{7x} - \frac{4}{3x} > 1$  [4]

B7(a) Differentiate the following functions with respect to  $x$

(i)  $y = 3x^2 + 2x + 7 + e^{3x^2 - 3x + 6}$  [4]

(ii)  $x = t - \frac{1}{t}$  and  $y = \frac{1}{t^2}$  [4]

(iii)  $y = \frac{1}{x^2}$  [2]

b) Integrate the following functions with respect to  $x$ .

i)  $\frac{\cos x - \sin x}{\sin x + \cos x}$

ii)  $3e^{-3x} - \frac{1}{2}e^{2x}$

iii)  $(3x + 5)^5$

iv)  $\cos(6 - 7x)$  [10]

B8 a) Find the area of the bounded plane region R lying between the curves

$y = x^2 - 2x$  and  $y = 4 - x^2$  [5]

(b) Given that  $x = 3(2\theta - 3\sin 2\theta)$  and  $y = 3(1 - \cos 2\theta)$

Find  $\frac{dy}{dx}$  [5]

(c) Find the equation of the tangent to the curve  $3x^2 - 7y^2 + 4xy - 8x = 0$  at the point  $(-1, 1)$ . [5]

(d) (i) Define  $\cosh x$  and  $\sinh x$  in terms of exponentials.

(ii) Using the definition in (i) above show that

$\frac{d}{dx} \cosh(x) = \sinh(x)$  [5]

B 9. (a) Deduce the formula for the sum  $\frac{1}{1.2} + \frac{1}{2.3} + \dots + \frac{1}{n(n+1)}$  and prove it by

induction [7]

(b) (i) Integrate  $x^2 e^x$  with respect to  $x$  [3]

(ii) Express  $\frac{2x-3}{x^2-5x+6}$  in partial fractions hence or otherwise

$\int_0^1 \frac{2x-3}{x^2-5x+6} dx$  [4, 6]

**END OF QUESTION PAPER**